

JHARSUGUDA ENGINEERING SCHOOL

DEPARTMENT OF MECHANICAL ENGINEERING



Lecturer notes on

THERMAL ENGINEERING-1

(3rd semester)

Subject code-Th-4

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Thermal Engineering - I

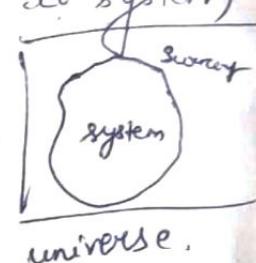
Thermodynamic system :-

A thermodynamic system is defined as any region of space or a finite quantity that occupies a volume & has a boundary.

e.g. - gas cylinder of reciprocating engine.

Surroundings :- Anything external to system

system + surroundings = universe.



Types of thermodynamic system

- (1) Closed system → mass constant, mass can't transfer
→ Heat & work transfer.
energy

e.g. - tea kettle.

- (2) Open system → mass, energy cross the boundary of system.

e.g. Reciprocating compressor, boilers, turbines.

- (3) Isolated system :- Both mass & energy can't transfer from the system.

e.g. - universe, thermoflask.

- (4) Adiabatic system :- thermally insulated from its surroundings

→ work transfer but not heat.

Thermodynamic Properties of system

P, V, T, entropy, enthalpy, Internal energy.

Pressure:-

→ it define as force per unit area.

→ unit = pascal

$$1\text{ Pa} = 1 \text{ N/m}^2$$

$$1 \text{ bar} = 1 \times 10^5 \text{ N/m}^2 = 100 \text{ kPa} = 0.1 \text{ MPa}$$

Atmospheric pressure:-

atm pressure = ~~root~~ Pressure due to
the wt. of the column of air
above the earth surface.

std. pressure = 760 mm of Hg at 0°C at
= 1.013 bar at sea level.

$$\begin{aligned}\text{Atm pressure} &= 1.013 \times 10^5 \text{ N/m}^2 \\ &= 101.3 \times 10^3 \text{ N/m}^2 = 101.3 \text{ kPa}.\end{aligned}$$

$$\checkmark 1 \text{ mm of Hg} = \frac{101.3 \times 10^3}{760} = 133.3 \text{ N/m}^2.$$

Gauge pressure:-

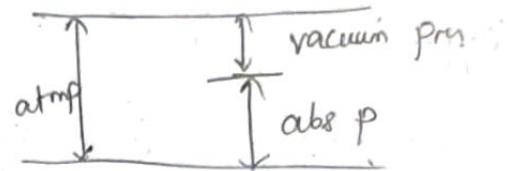
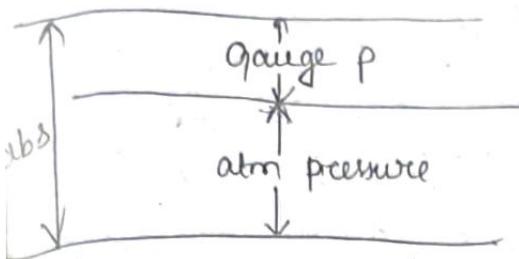
when instrument records pressure
above atm pressure.

Vacuum pressure:-

records pressure below atm
pressure (-ve gauge pressure)

$$\text{Abs pressure} = \text{Gauge p} + \text{atm p}$$

$$= \text{atm p} - \text{vacuum p}$$



Temp (T)

→ define as degree of hotness or coldness of a body or environment.

$$K = {}^{\circ}\text{C} + 273$$

(v) volume :- (v) The amt of space occupied.
unit = l, m³

(s) entropy :- Entropy is the loss of energy available to do work. entropy is a measure of randomness. (s) (J/K)

enthalpy & internal energy : (U) (J/K)

of a thermodynamic system is the energy contained within it.

$$\rightarrow U \uparrow, T \uparrow, \Delta U = q + w$$

(H) Enthalpy :- sum of internal energy
product of P & V

$$H = U + PV \quad (\text{J/kg})$$

Thermodynamic properties

Every system has some characteristic by which its physical condition describe such as $P, V, T \rightarrow$ These are called properties of system.

Thermod 2 types of properties

- (1) Intensive property. \leftarrow independent of mass e.g. = $P, V, S.P. energy, S.P. volume, density$
- (2) Extensive property.

\uparrow depend on the mass

e.g. - volume, total energy.

Thermodynamic process

any properties of system changes \rightarrow change of state \rightarrow \uparrow thermodynamic process.

e.g. \rightarrow expansion of gas as it flow through turbine.

(1) Isochoric process \rightarrow process take place at constant volume.

(2) Isobaric process \rightarrow const. pressure.

(3) Isothermal \uparrow \rightarrow

Thermodynamic cycle :-

process are performed on a system in such a way that the final state is identical with initial state, without change of physical properties.



Phase

quantity of matter which is homogeneous (uniform) throughout in physical struc. & chemical composition.

3 phase - solid, liquid, gas.

Homogeneous & Heterogeneous system :-

Single phase → Homogeneous → e.g. water, ice, water vapour, mixture of ammonia on H_2O .

more than one phase → Heterogeneous system
e.g. - water + steam
ice + H_2O
water + O₂.

Thermodynamic State & path

→ state :- condition of physical existence of a system at any instant of time.

→ it is described by properties such as P, T, V etc.

→ system undergoes a change of state without change of phase.

→ Thermodynamic system passing through a series of states constitutes a path.

Thermodynamic equilibrium

3 equilibria satisfied.

- ① mechanical \leftarrow no unbalance force
- ② chemical \leftarrow no chemical reaction
- ③ thermal \leftarrow no temp difference.

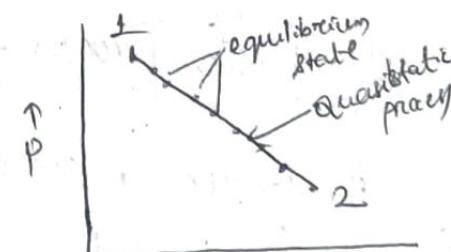
Quasi-static process

Quasi-static process is one in which the system deviates from thermodynamic equilibrium state by only infinitesimal amount throughout the entire process.

→ This process may, practically, be considered as a series of equilibrium states & its path may represent graphically as continuous line on a state diagram.

Reversible process

process which can be reversed in direction and the system follows same continuous series of equilibrium state \rightarrow is said to be reversible process.



\Rightarrow Quasi-static process \rightarrow Reversible process

- it exists when there is no friction.
- no heat transfer across finite temp difference.
- For actual, reversible process cannot exist.

Irreversible process

- will not retrace the reverse path.



Heat

Energy interaction between system & surroundings

(joules J) (KW)

Heat transfer 3 ways

① Conduction

② Convection

③ Radiation



Specific Heat

amount of heat required to raise the temp of unit mass of a substance through 1°C .

unit - $\text{kJ/kg} \cdot \text{K}$

$$Q = m c (T_2 - T_1) \text{ in kJ}$$

$m = \text{mass (kg)}$

$c = \text{specific heat (kJ/kg} \cdot \text{K})$

$T_1 = \text{initial temp}$

$T_2 = \text{final temp.}$

→ Solid, liquid → one specific heat

→ Gas → at const pressure $\rightarrow C_p$

→ " const volume $\rightarrow C_v$

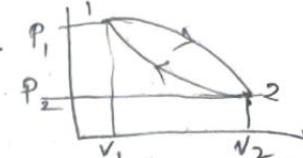
$$C_p > C_v$$

$$\frac{C_p}{C_v} = \gamma$$

Point function :-

when a thermodynamic property has a definite value for a given state, it is called point functⁿ.

e.g. = P, V, T



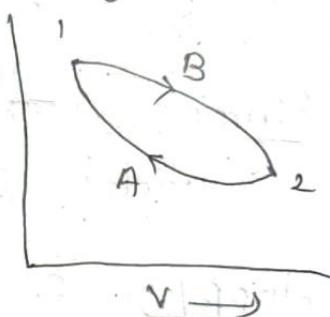
→ it depends on initial & final states of the system.

Path function

the quantities which are not thermodynamic properties, are known as path functions.

e.g. = Heat, Work.

1-B-2 → 2-A-1



Comparison

between Heat & work

Similarities

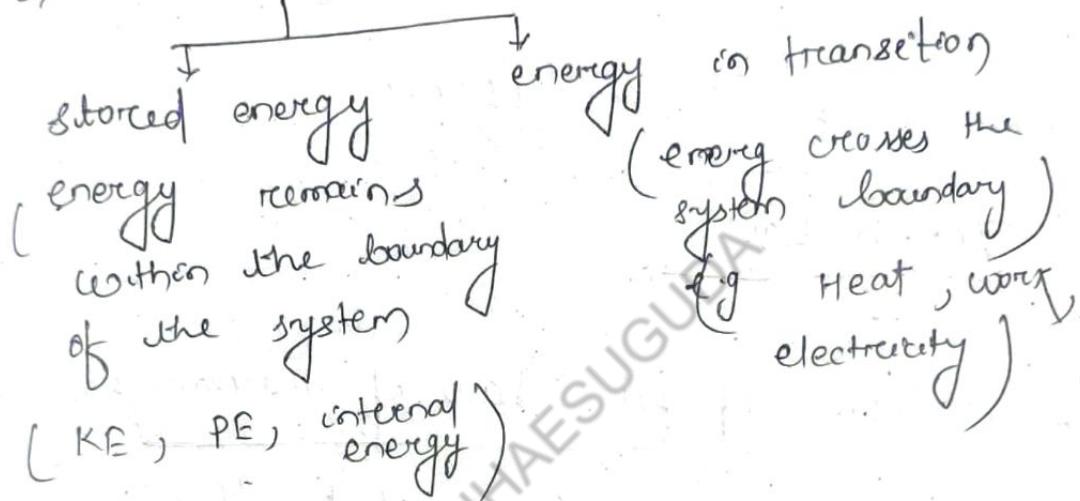
- ① Heat & work both are boundary phenomena. they are observed at boundary of system.
- ② Both are transient phenomena. do not possess heat & work.
- ③ Both are represent energy crossing the boundary of system.
- ④ Both are path function. exact differential thermodynamic properties.

Differences :-

- (1) In stable system, no reversible work transfer but heat transfer takes place.
- (2) for transfer of heat, temp difference needed.

Energy :- (E) defined as capacity to do work.
unit = N-m

→ ~~Q~~ 2 types



Different forms of stored energy :-

① potential Energy :- energy possessed by a body

$$P.E = mgh \quad (\text{J})$$

② K.E = energy possessed by a body or system by virtue of its mass & velocity of motion.

$$K.E = \frac{1}{2}mv^2 \quad (\text{J or N-m})$$

③ internal Energy :- " " by a body or a system by virtue of its molecular arrangement & motion of molecules.

TT UP

Work, heat & comparison b/w two

Heat :- Heat is energy interaction bet' the system & surrounding.

→ it defined as the energy transferred, without transfer of mass, across the boundary of a system due to temp difference bet' the system & surrounding.

3 ways heat transfer :-

(1) Conduction :- process of heat transfer from one particle to another particle of the body, in the direction of fall of temp.

2) convection :- heat transfer from one particle to another particle of the body by convection currents in fluid.

3) Radiation :- heat transfer without affecting intervening medium.

→ if heat flow into a system from surroundings = +ve, \dot{Q}
from system to surroundings = -ve $\rightarrow \dot{Q}$

Work: Energy transferred across the boundary of a system between system & surrounding.

→ work done by the system on surroundings = $+W$ (driving expand position)
 → from suc to sys = $-W$ (rotating carded)

Comparison of Heat & Work

Similarity: ~~in wavy lines~~ both boundary phenomena.

- (1) heat & work are both transient phenomena.
- (2) The heat & work are both transient phenomena.
- (3) when a system undergoes a change, heat transfer or work done may occur at the boundary.
- (4) The heat & work represent the energy crossing the boundary of the system.
- (5) Heat & work both are path function & depend upon the forces.
- (6) Both are exact differential.

Difference:

- (1) For the transfer of heat, the temp difference is needed.
- (2) In stable system there can't be work transfer but there is no restriction for heat transfer.

exact $\oint p \cdot dV = 0$ (cycle change of variable $\oint = 0$)

exact diff = $\oint \delta q = 0$

Work transfer \rightarrow displacement work

displacement work

Let $A = \text{area of piston}$

pressure force exerted by the gas on piston

$$= F_p = (P \cdot A)$$

then it give small \rightarrow displacement $= dl$

because of displacement there is small work is done

$$dw = F_p \cdot dl$$

$$= P \cdot A \cdot dl$$

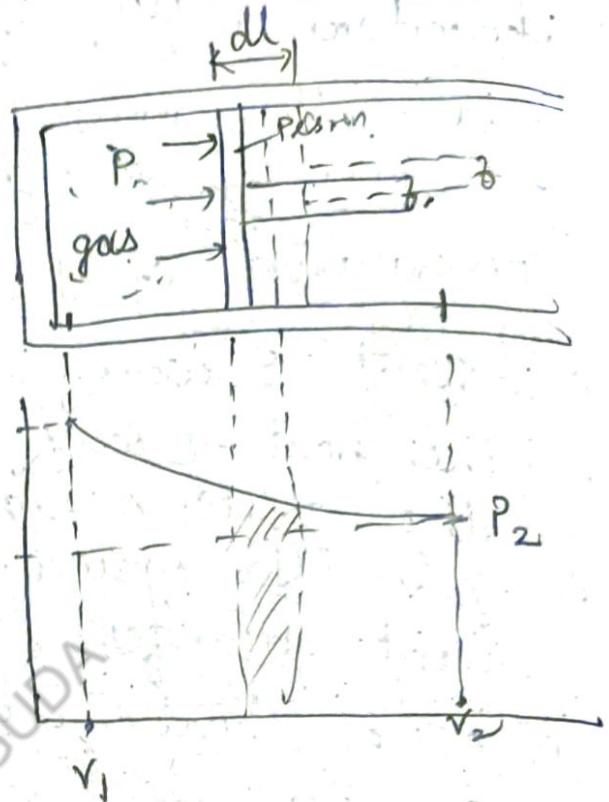
$$dw = P \cdot dV$$

small elementary work

total work done moving from 1 to 2
you have to integrate

$$\int_{V_1}^{V_2} dw = \int_{V_1}^{V_2} P dV$$

$$w_{12} = \int_{V_1}^{V_2} P dV$$

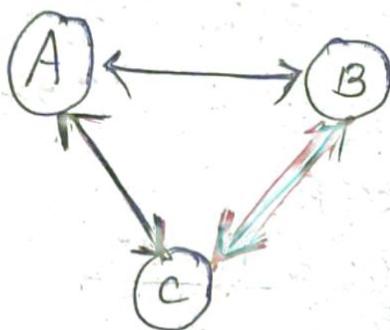


Laws of Thermodynamics

Zerath law of Thermodynamics

when two systems are each in thermal equilibrium with a third system, then they are also in thermal equilibrium with each other. The statement is known as Zerath law of thermodynamics.

e.g.:



temp → defined as the degree of hotness or coldness of a body or environment

→ Two body are in contact \Rightarrow heat transfer from hot body at high temp to a cold body at lower temp.

→ for measuring ~~ordinary~~ ordinary temp Thermometers use.

→ for measuring high temp — pyrometer.

→ If gas will not occupy any volume at a certain temp. This temp known as absolute zero temp.

— absolute temp = thermometer's reading + 273 °C

temp measuring scale

(1) celsius & Fahrenheit scale

→ it has two fixed point → celsius scale

(1) Freezing point of water (0°C) ← ice point

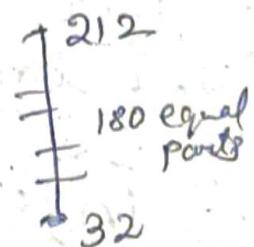
2) Boiling point of water (100°C) ← steam point

* Fahrenheit scale

→ Freezing point = 32

→ Boiling point of H_2O = 212

→ ${}^{\circ}\text{F}$



Relation betⁿ celsius & F

$$\rightarrow \frac{C}{100} = \frac{F-32}{180} \quad \text{or} \quad \frac{C}{5} = \frac{F-32}{9}$$

* ~~c & F scale show same reading~~

$$\text{at } -40^\circ\text{C} \quad \boxed{-40^\circ\text{C} = -40^\circ\text{F}}$$

First law of Thermodynamics

first law of thermodynamics for a closed or non-flow system undergoing cycle according to 1st law of thermodynamics, the heat & mechanical work are naturally convertible.

→ when a closed & non-flow system undergoes a thermodynamic cycle, the heat transfer is equal to net work transfer.

$$\int dQ = \int dw$$

$$\int dQ - \int dw = 0$$

Limitation of 1st Law of Thermodynamics

- ① we know $\int Q = \int W$, but this statement doesn't specify the direction in which heat & work flows.
- a) ~~Reversible~~ Heat energy & mechanical work are mutually convertible. Mechanical energy fully converted into heat energy, but a part of heat energy converted into mechanical work.

thermodynamics

(1) A closed system consist of water on a cylinder. Heat given to the system is cylinder 45 kJ and it that 40 kJ of heat done by the cylinder. determine the change in internal energy during this process.

$$\therefore Q = 45 \text{ kJ}$$

$$W = -40 \text{ kJ}$$

$$Q = U + W$$

$$U = Q - W = 45 - 40 = 5 \text{ kJ}$$

(2) A closed system consist of water on a cylinder and being stirred by a paddle wheel, during the process 35 kJ/h of work given to the system and internal energy increases to 145 kJ from initial value of 120 kJ during the of stirring determine heat transfer. as the temp raising or falling.

$$W = -35 \text{ kJ/h}$$

$$\rightarrow U_2 = 145 \quad U_1 = 120$$

$$dU = U_2 - U_1 = 145 - 120 = 25 \text{ kJ/h}$$

$$Q_{1-2} = U_{12} + W_{12} = 25 + 35 = 60 \text{ kJ/h}$$

$U \uparrow T \uparrow$

Classification of thermodynamic processes

① Closed or non-flow process :-

- No transfer of mass across the boundary
- Energy in form of heat & work
- Can transfer.

2) Open or flow process :-

- Transfer of mass to & from the system.
- Mass enter the system & leaves after exchanging the energy.
- e.g. Turbines, compression.

Workdone for a closed or non-flow process :-

→ Consider a system (gas) enclosed in cylinder, piston arrangement.

→ Let at state 1, etc in equilibrium state.

$$P_1, V_1, \theta_1$$

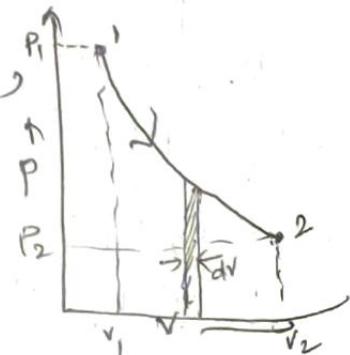
→ at position 2, ~~etc~~ etc P_2, V_2

→ Force acting on the piston,

$$F = P.A$$

Force causes the piston to move through a small distance dz .

$$\text{Workdone} = F \times dz$$



$$\delta w = P \cdot A \cdot dV = P \cdot dV \quad \text{--- (1)}$$

dV = change in volume = $A \cdot dV$.

when gas expand from 1 to 2.

$$W_{1-2} = \int_1^2 \delta w = \int_1^2 P \cdot dV \quad \text{--- (II)}$$

$$W = \int_1^2 P \cdot dV$$

- Q) A perfect gas expands in such a way that its pressure varies in a linear relationship with volume.

$$P = av + b, \quad a, b = \text{constant.}$$

If initial and final states of the gas are 4 bar, 0.1 m^3 and 2 bar, 0.2 m^3 ; determine work of interaction.

$$\rightarrow P_1 = 4 \text{ bar} \xrightarrow{\text{1000 KN/m}^3} V_1 = 0.1 \text{ m}^3$$

$$P_2 = 2 \text{ bar}, \quad V_2 = 0.2 \text{ m}^3 \\ = 200 \text{ KN/m}^3$$

$$P_1 = av_1 + b \quad \text{--- (1)}$$

$$400 = a \times 0.1 + b = 0.1a + b \quad \text{--- (1)}$$

$$P_2 = av_2 + b$$

$$200 = 0.2a + b \quad \text{--- (II)}$$

$$0.1a + b = 400$$

$$0.2a + b = 200$$

$$a = -2000 \quad b = 600$$

$$\delta w = \int_{V_1}^{V_2} P dV$$

$$\delta w = \int_{V_1}^{V_2} (av + b) dV$$

$$w_{1-2} = \left[\frac{av^2}{2} + bv \right]_{V_1}^{V_2} = \left[\frac{-2000v^3}{2} + 600v \right]_{V_1}^{V_2}$$

$$= \left[-1000v^2 + 600v \right]_{0.1}^{0.2}$$

$$= 30 \text{ kJ}$$

Types of Non-flow processes

① Reversible non-flow process

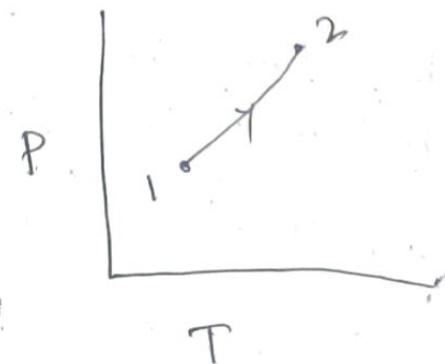
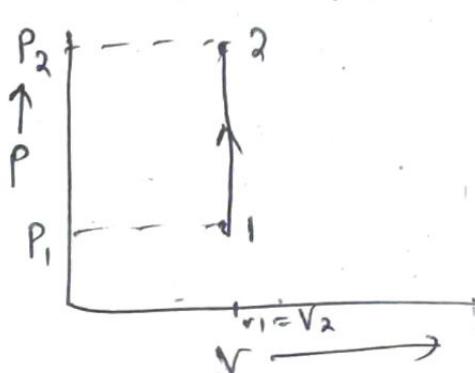
- a) const. volume process (isochoric)
- b) const. P (isobaric)
- c) const. T (isothermal)
- d) adiabatic
- e) ~~no~~ polytropic process.

② Irreversible non-flow process

const. volume process (isochoric)

volume of gas remain constant.

heat supply \rightarrow increase P & T .



$$P_1, V_1, T_1 = \text{at state 1}$$

$$P_2, V_2, T_2 = " " " 2.$$

$$V_1 = V_2$$

according to Charles Law

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

work done by gas $\delta w = P dV$.

$$\int dW = \int P dV = P \int_{1}^{2} dV$$

$$w_{1-2} = P(V_2 - V_1) = 0 \quad \text{as } (V_1 = V_2)$$

$$w = 0.$$

2) change in internal energy.

$$dU = mC_V dT$$

$$\left\{ \begin{array}{l} dU = \int mC_V dT = mC_V \int_{1}^{2} dT \\ U_2 - U_1 = mC_V (T_2 - T_1) \end{array} \right.$$

3) Heat transfer

$$dQ = dU + dw$$

$$Q_{1-2} = U_2 - U_1 + 0 = mC_V (T_2 - T_1)$$

3) change in enthalpy. $(P_1 V_1 = mRT_1)$

$$dH = dU + d(PV)$$

$$H_2 - H_1 = mC_V (T_2 - T_1) + (mRT_2 - mRT_1) \quad (C_P - C_V = R)$$

$$= mC_V (T_2 - T_1) + mR (T_2 - T_1)$$

$$= mC_P (T_2 - T_1)$$

Application of 1st law of thermodynamics

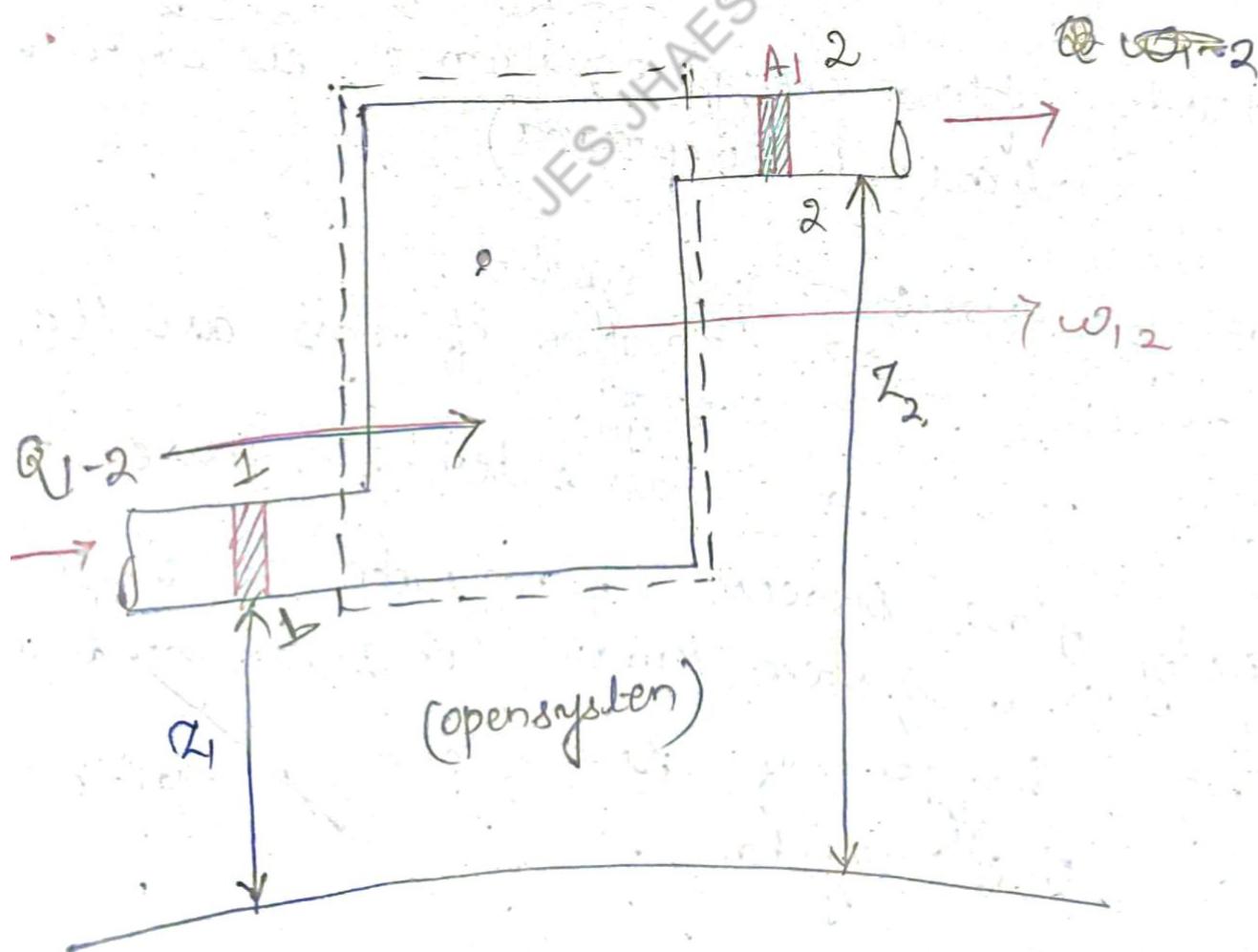
(Steady flow energy equation & its application
to turbine & compressor)

- * flow processes :-
 → open system
 → transfer of mass as well as energy.
 → mass enter = mass exist
- * steady flow process = flow rate in & out
 of the system remain constant with time.
 → no change of stored energy within
 the system.

unsteady flow process :-

- Working substance varies with time.
- mass inflow ≠ mass outflow
- * We mostly dealing with steady flow process
- * $\rightarrow m_i = m_o \text{ & } m = C$
- $\rightarrow Q = 0 \text{ & } \omega = 0$
- \rightarrow working substance = uniform composition

1st law of Thermodynamic applied to
steady flow process :-



working substance enter at 1-1,

with velocity v_1 & p_1 ,

specific volume & specific internal energy
(v_{s1}) (u_1).

2-2 velocity v_2 , pressure p_2

specific volume = v_{s2} specific internal = u_2
energy

→ heat transfer = q_{12}

→ work transfer = w_{12}

⇒ (1) $m_1 = m_2$ (per unit

(2) Energy = necessary to determine the energy
therefore flow per unit mass flowing at various
position of the open system.

→ energy accompanying unit mass flow
consist of following parts.

(i) PE = gZ (Z = height from datum plane)

(ii) KE = $\frac{V^2}{2}$

(iii) internal Energy ' u'

(iv) flow energy = $P v_s$

According to 1st law of thermodynamic
law of conservation of energy.

$$E_i = E_o$$

$$\boxed{E_1 = E_2} \quad \text{--- } ①$$

$E = PE + KE + U + \text{flow energy}$

for inlet energy enter to system

$$E_1 = gz_1 + \frac{v_1^2}{2} + u_1 + q_{12} + p_1 v s_1 \quad ②$$

at exist energy leaving the system

$$E_2 = gz_2 + \frac{v_2^2}{2} + u_2 + w_{12} + p_2 v s_2 \quad ③$$

eqn ①

$$E_1 = E_2$$

$$gz_1 + \frac{v_1^2}{2} + u_1 + q_{12} + p_1 v s_1 = gz_2 + \frac{v_2^2}{2} + u_2 + w_{12} + p_2 v s_2$$

$$gz_1 + \frac{v_1^2}{2} + (u_1 + p_1 v s_1) + q_{12} = gz_2 + \frac{v_2^2}{2} + (u_2 + p_2 v s_2) + w_{12}$$

$g z_1 + \frac{v_1^2}{2} + h_1 + q_{12} = g z_2 + \frac{v_2^2}{2} + h_2 + w_{12}$

~~This eqⁿ called as steady flow energy eq.
(SFEF)~~

* This can also be written as

$$\begin{aligned} q_{12} - w_{12} &= g(z_2 - z_1) + \left(\frac{v_2^2 - v_1^2}{2} \right) + (h_2 - h_1) \\ &\quad (\text{J/kg}) \quad (\text{J/kg}) \quad (\text{m}) \\ &= (PE_2 - PE_1) + (KE_2 - KE_1) + (h_2 - h_1) \end{aligned}$$

in differential form.

$$\delta q - \delta w = d(PE) + d(KE) + dh$$

Q) In a certain steady flow process, the properties of the fluid at inlet & outlet are follows.

→ inlet. $P = 1.5 \text{ bar}$, $\rho = 26 \text{ kg/m}^3$, $V = 110 \text{ m/s}$, internal energy = $q_{10} = 910 \text{ kJ/kg}$

exist:- $P = 5.5 \text{ bar}$, $\rho = 5.5 \text{ kg/m}^3$, $V = 190 \text{ m/s}$, $U = 710 \text{ kJ/kg}$.

during process fluid rejects 55 kJ/s heat & rises through 155 m ; mass flow rate of the fluid 10 kg/min .

Determine

- (1) change in Enthalpy.
- (2) power developed during the process.

$$\text{Ans} \quad P - P_1 = 1.5 \text{ bar} = 150 \times 10^3 \text{ N/m}^2 = 150 \text{ kN/m}^2$$

$$(1 \text{ bar} = 10^5 \text{ N/m}^2 = 0.01 \text{ MPa} = 100 \text{ kPa})$$

$$1 \text{ Pascal} = 1 \text{ N/m}^2$$

$$f_1 = 1.5 \text{ kg/m}^3 \cdot 26 \text{ kg/m}^3$$

$$V_{B1} = \frac{1}{f_1} = \frac{1}{26} = 0.038 \text{ m}^3/\text{kg}$$

$$V_1 = 110 \text{ m/s}$$

$$u_1 = 910 \text{ kJ/kg}$$

outlet

$$P_2 = 5.5 \text{ bar} = 550 \times 10^3 \text{ N/m}^2 = 550 \text{ kN/m}^2$$

$$f_2 = 5.5 \text{ kg/m}^3$$

$$V_{B2} = \frac{1}{f_2} = \frac{1}{5.5} = 0.182 \text{ m}^3/\text{kg}$$

$$V_2 = 190 \text{ m/s}$$

$$u_2 = 710 \text{ kJ/kg}$$

$$Q_{12} = 55 \text{ kJ/s}$$

$$Z_2 = 55 \text{ m}$$

$$\text{mass of fluid rate} = 10 \text{ kg/min} = \frac{10}{60} = \frac{1}{6} \text{ kg/s.}$$

(1) change in enthalpy:

$$\text{inlet enthalpy } h_1 = u_1 + p_1 V s_1 = 910 + 150 \times 0.038 \\ = 915.7 \text{ kJ/kg}$$

$$\text{exit } " \quad h_2 = u_2 + p_2 V s_2$$

$$h_2 = 710 + 550 \times 0.182 = 810.1 \text{ kJ/kg}$$

$$dh = h_2 - h_1 = 810.1 - 915.7 = -105.6 \text{ kJ/kg}$$

2) power developed during the process? -

Let w_{12} = work done or power developed
during the process in kJ/kg
heat rejected by the fluid

$$q_{12} = \frac{w_{12}}{m} = \frac{-55}{1/6} = -55 \times 6 = -330 \text{ kJ/kg}$$

(-ve sign due to heat rejection)

Steady flow energy eqn.

$$q_{12} - w_{12} = g(z_2 - z_1) + \left(\frac{V_2^2 - V_1^2}{2} \right) + (h_2 - h_1)$$

$$-330 - w_{12} = \frac{9.81}{1000} (55-0) + \left(\frac{(90)^2 - (10)^2}{2 \times 1600} \right) + (-105.6)$$

$$w_{12} = -330 + 93.06 = -236.94 \text{ kJ/kg.}$$

Since the mass flow rate $\frac{1}{6} \text{ kg/s}$, therefore work done or power developed during process.

$$W_{12} = m \times w_{12} = \frac{1}{6} (236.94) = 39.5 \text{ kJ/s} \\ = 39.54 \text{ kW}$$

(i) An fan is to accelerate air to velocity of 10 m/s delivering the air at the rate of $4 \text{ m}^3/\text{s}$. if the density of air 1.18 kg/m^3 . determine the min power that must be supplied to fan.

$$v = 10 \text{ m/s}$$

$$\text{Volume } V = 4 \text{ m}^3/\text{s}$$

$$\rho = 1.18 \text{ kg/m}^3$$

mass of air supplied by the fan

$$m = \rho \times V = 4 \times 1.18 = 4.72 \text{ kg/s}$$

KE imparted by the fan to the air

$$\frac{1}{2}mv^2 = \frac{1}{2} \times 4.72 \times (10)^2 = 236 \text{ J/s.}$$

so power supplied to the fan $(1 \text{ Nm} = \text{J/s})$

$$\text{fan} = 236 \text{ Wj/s.}$$

Q) For a steady flow process

A closed system consisting of water contained in a cylinder & being stirred by a paddle wheel. During process 35 kJ/h of work was imparted to the system & the internal energy is increased to 145 kJ from an initial value of 120 kJ during one hour of stirring. Determine heat transfer & the system temp rising rate?

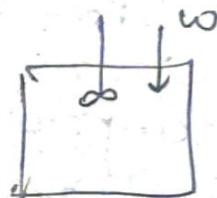
$$\rightarrow w_{12} = -35 \text{ kJ/h}$$

$$U_2 = 145 \text{ kJ} \quad U_1 = 120 \text{ kJ}$$

$$\Delta U = U_2 - U_1 = 145 - 120 = 25 \text{ kJ/h}$$

$$Q_{12} = \Delta U + w_{12}$$

$$\therefore Q_{12} = 25 - 35 = -10 \text{ kJ/h}$$



Q) The gas is compressed from an initial state of 0.35 m^3 & 105 kPa to a final state of 0.14 m^3 & to the same pressure. Determine change in internal energy of the gas which transfers -38 kJ of heat.

$$\rightarrow V_1 = 0.35 \text{ m}^3 \quad P_1 = 105 \text{ kPa}$$

$$V_2 = 0.14 \text{ m}^3 \quad P_2 = 105 \text{ kPa}$$

$$U = ? \quad Q = -38 \text{ kJ}$$

$$\begin{aligned} W = \int P dV &= P(V_2 - V_1) = 105 \times 10^3 (0.14 - 0.35) \text{ Nm} \\ &= -22.05 \times 10^3 \text{ N-m} \\ &= -22.05 \text{ kJ} \end{aligned}$$

Now $\eta \quad d\eta = du + dw$

$$\therefore -38 = du - 22.05$$

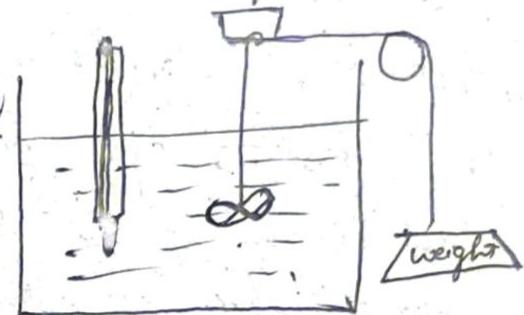
$$\therefore du = -15.95 \text{ kJ}$$

\therefore negative sign indicate that there is decrease in internal energy.

Mechanical Equivalent of Heat

Let us consider a closed system which consists of mass of water contained in a adiabatic vessel having a thermometer & paddle wheel.

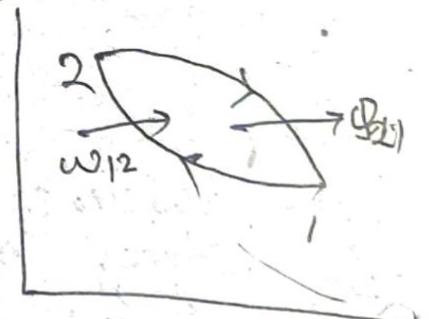
→ Let w amount of work done on the system by paddle wheel. quantity of work can be measured by the fall of weight.



- system initially at temp t_1 temp rise t_2 .
- let ~~not~~ insulation now removed, system & surrounding interacted by heat transfer till returns to its original temp t_1 attaining condition of thermal equilibrium
- work done always proposional to heat.

$$\sum w \propto q$$

$$(\sum w) = j (\sum q)_{\text{cycle}}$$



J : joule equivalent or mechanical equivalent of heat. $j = \frac{w}{q}$

- work was transferred to the measured mass of water by means of paddle wheel driven by the falling weight.

4a-2 Second Law of Thermodynamics

b-2

c-1 According to 1st Law of Thermodynamics limitation it don't specify the direction in which Heat & work flow.

→ According to 2nd Law of Thermodynamics the whole of heat energy can't be converted into work & part of energy must be rejected to surrounding.

Statements of 2nd Law of Thermodynamics

(1) Kelvin - Planck statement :-

"it is impossible to construct an engine which, while working in a cycle, produces no effect other than to extract heat from a single thermal reservoir & perform an equivalent work".

→ efficiency $\frac{Q_f - Q_o}{Q_f} \times 100\%$

Clausius statement :-

"it is impossible to construct an engine which, while working in a cycle, produce no effect other than to transfer heat from a low temp reservoir to high temp reservoir".

without aid of an external agency.

→ PMM - I , PMM - II
 (violet law) (violet Kelvin-Planck statement)
terms used

(1) Thermal or Heat reservoir:-

The thermal or heat reservoir is a system or body of extremely large heat capacity, capable of absorbing or rejecting finite amount of heat without any change in temp.

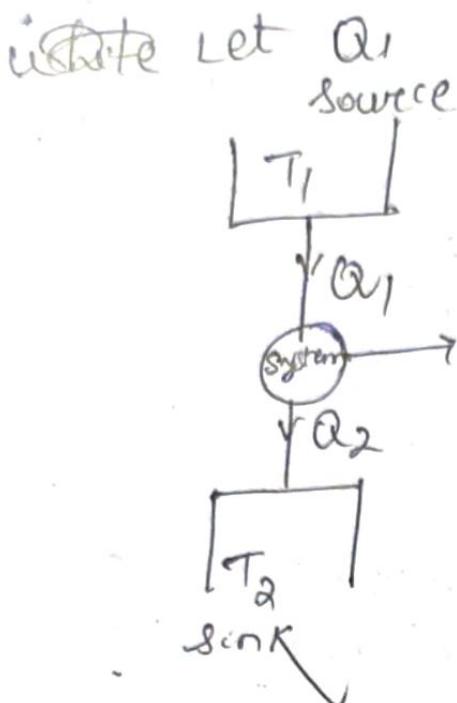
e.g. - river, sea, atmosphere.

2) Heat source :- it is a reservoir at a high temp which heat extracted without change of its temp.

e.g. sun, boiler furnace, nuclear reactor.

3) Heat sink :- it is a reservoir at a low temp. it is capable of absorbing any amount of heat without change in temp.

4) Heat Engine :- A Heat engine is a thermodynamic system used for converting heat into work while operating in a cycle between source & sink.



$Q_1 - Q_2 = (W_E)$ work done by the system.

→ performance of heat Engine is measured by the its efficiency.

efficiency of heat Engine (η_E)

$$\eta_E = \frac{\text{Net work done}}{\text{Total heat supplied}}$$

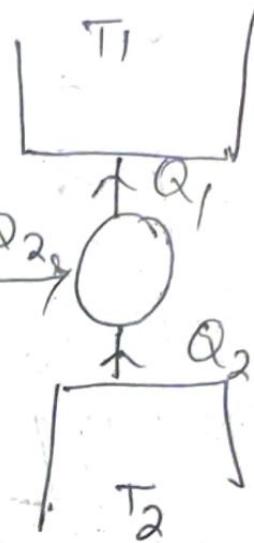
$$= \frac{W_E}{Q_1} = \frac{Q_1 - Q_2}{Q_1} = 1 - \frac{Q_2}{Q_1}$$

for a reversible engine = $\frac{Q_2}{Q_1} = \frac{T_2}{T_1}$

$$80 \quad \eta_E = 1 - \frac{Q_2}{Q_1} = 1 - \frac{T_2}{T_1}$$

⑤ Heat pump :-

it is a thermodynamic system used for extracting low temp body & delivered it to a high temp body.



Let 'Q₂' amount of heat is extracted from sink

having temp T_2

~~higher temp~~

& supply heat Q_1 to a

body at high temp T_1 by

using external energy in the form of work input (w_r)

The performance of heatpump measured by the co-efficient of performance

$$\text{e.g. } (\text{cop})_{\text{HP}} = \frac{\text{Heat supplied}}{\text{External work supplied}}$$

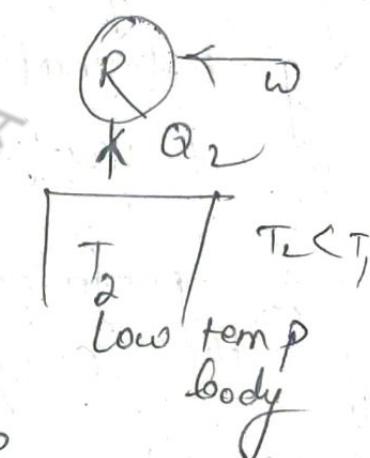
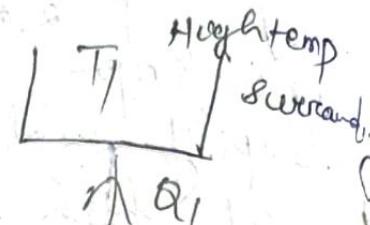
$$= \frac{Q_1}{W_r} = \frac{Q_1}{Q_1 - Q_2} = \frac{T_1}{T_1 - T_2}$$

Heat pump is used to keep room warm in winter.

Q) Refrigerator: it is a device similar to heat pump, which extract heat from lower temp body & delivers it to a high temp body.

Let Q_2 is extracted from space to be cooled at temp T_2 which is lower than temp of the surrounding & reject Q_1 to the surrounding at temp T_1 .

→ The refrigerator, while operating in a cyclic process, require an input work (w) to transfer heat from a low temp to a high temp.



$$(COP)_R = \frac{\text{Heat extracted}}{\text{Work input}} = \frac{Q_2}{w} = \frac{Q_2}{\frac{Q_2 - Q_1}{C_p}} = \frac{Q_2}{Q_2 - Q_1} = \frac{T_2}{T_1 - T_2}$$

Relation betw (COP)_R & (COP)_{HP}

$$(COP)_R = \frac{T_2}{T_1 - T_2} \quad (COP)_{HP} = \frac{T_1}{T_1 - T_2}$$

$$(COP)_R + 1 = \frac{T_2}{T_1 - T_2} + 1 = \frac{T_1}{T_1 - T_2} = (COP)_{HP}$$

$$(COP)_P = (COP)_R + 1$$

Chapter -3

Properties process of perfect gas

① gas → complete vapourisation of liquid
 vapour → partially vapourisation " "

② ideal or perfect gas | real gas

→ strictly obey the gas laws under all cond' of temp & pressure. | → not obey

→ st. always remains in gaseous state.

e.g. - O₂, N₂, air.

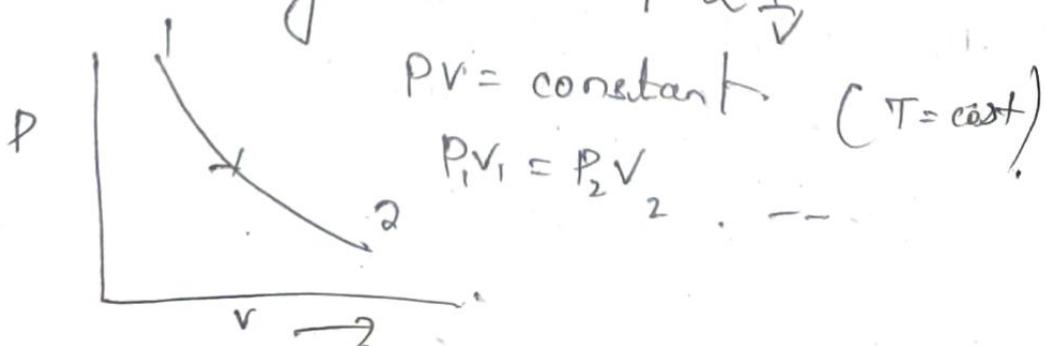
(3) Boyle's Law

→ 1662, Robert Boyle.

→ He found that when a gas is heated at const. temp., pressure multiplied by the volume remain constant.

→ Or we can say 'V' of a given mass of a perfect gas varies inversely w/ absolute temp T const.

$$\text{PQD} \text{ Boyle's Law} = P \propto \frac{1}{V}$$



Charles's Law \rightarrow 1787, A. C. Charles.

v of a perfect gas varies directly as its absolute temp, when absolute p const.

$$\sqrt{dT}, \frac{V}{T} = \text{const} \quad (P = \text{const})$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2} = \frac{V_3}{T_3} = \text{const}$$

$$\rightarrow P dT, \frac{P}{T} = \text{const}$$

$$\frac{P_1}{T_1} = \frac{P_2}{T_2} = \frac{P_3}{T_3} = \text{const}$$

Gay Lussac & Regnault Law

"All perfect gases expand by the same fraction of the volume they occupy at freezing temp, when their temp is raised by y° provided the pressure remains const."

\rightarrow fraction is found to be $\frac{1}{273}$ at 0°C .

V_0 = volume of a given mass of gas at freezing temp (0°C)

V_t = " of the same gas at $t^{\circ}\text{C}$.

$$V_t = V_0 + \frac{1}{273} V_0 t \Rightarrow V_t = V_0 \left(\frac{273+t}{273} \right) = V_0 \frac{T}{T_0}$$

$$\boxed{\frac{V_t}{V_0} = \frac{T}{T_0}}$$

T = absolute temp $\otimes t^{\circ}\text{C}$.

T_0 = " 0°C .

Combination of Boyle's & Charles' Law
(General gas eq)

$$V \propto \frac{1}{P} \quad (T=c) \quad (\text{Boyle's Law})$$

$$V \propto T \quad (P=c) \quad (\text{Charles' Law})$$

~~V $\propto \frac{1}{P}$~~

$$V \propto \frac{T}{P} \Rightarrow PV \propto T \quad \text{or} \quad PV = K \times T$$

$$\boxed{\frac{PV}{T} = K}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} = \frac{P_3 V_3}{T_3} = \text{const}$$

Joule's Law

It states that "the change in internal energy (dU) of a perfect gas is directly proportional to the change in temp (dT)."

$$dU \propto dT. \quad m = \text{mass of gas}$$

$$dU = m c (T_2 - T_1) \quad c = \text{const.} = \text{specific heat of a gas}$$

Characteristic eq of a gas

use known general eq of gas
 $PV = KT.$

for 1 kg mass $PV = RT.$

$$m \text{ kg mass} \quad \boxed{PV = mRT}$$

R = characteristic gas const. / gas const.

$$R = \frac{PV}{mT} = \frac{N \times m^3}{m^2 \times Kg \times K} = \frac{N \cdot m}{Kg \cdot K}$$

$$(1 \text{ o } N \cdot m = 1 \text{ J})$$

$$R = \frac{J}{Kg \cdot K}$$

R depends of types of gas.

$$\rightarrow \text{for atm air} = R = 287 \frac{\text{J}}{\text{kg} \cdot \text{K}} = 0.287 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$$

universal Gas const.

product of

$$R_u = R \cdot M$$

R = characteristic gas at
 M = molecular mass of gas.

$$R_u = R_1 M_1 = R_2 M_2$$

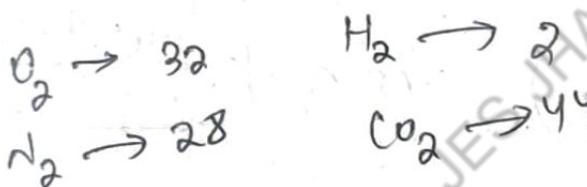
$$R_u = \text{same for all gas} = 8314 \frac{\text{J}}{\text{kg} \cdot \text{mole} \cdot \text{K}}$$

$$= 8.314 \frac{\text{kJ}}{\text{kg} \cdot \text{mole} \cdot \text{K}}$$

$$PV = MRT$$

$$PV = n \cdot R_u T$$

$n = \text{no. of kg moles}$



Avgadro's Hypothesis

"Equal volumes of all gases at the same P. & T. contain equal no. of molecules".

$$\frac{f_1}{f_2} = \frac{M_1}{M_2} \quad (P, T = \text{same})$$

$$\frac{f_1}{f_2} = \frac{1}{2}$$

Specific Heat of gas

it is defined as the quantity of heat required to raise the temp of 1 unit mass substance by 1° one degree

- solid, liquid $\rightarrow 1$ specific heat
- gas $\rightarrow 2$ specific heat

① specific heat const volume (c_v) (T, P)
(volume constant)

Q in kg of mass heated in closed vessel.

$$Q_{1-2} = m \times \text{mass} \times \text{specific heat at } V=C \times \text{rise in temp}$$

$$Q_{1-2} = m \times c_v \times (T_2 - T_1) = m c_v dT$$

2) specific heat const p $\nabla T P$.

$$Q_{1-2} = m c_p \times dT \quad Q_{1-2} = dU + W_{1-2} \\ = m c_v (T_2 - T_1) + P(V_2 - V_1)$$

Relationship between Two specific heat

① Difference betⁿ specific heat.

m kg mass \rightarrow heat at const P from temp T_1 to T_2 .

Heat supplied $Q = m c_p dT$

$$Q = dU + dW_{1-2} = dU + P dV$$

$$\therefore m c_p (T_2 - T_1) = m c_v (T_2 - T_1) + P(V_2 - V_1)$$

$$\therefore m(T_2 - T_1)[c_p - c_v] = (P V_2 - P V_1) \quad \left\{ \begin{array}{l} PV = mRT \\ P V_1 = m R T \\ P_2 V_2 = m R T \end{array} \right.$$

$$\therefore [T_2 - T_1](c_p - c_v) = m R (T_2 - T_1) \quad \boxed{c_p - c_v = R}$$

Ratio of specific heats :-

$$C_p - C_v = R$$

$$\frac{C_p}{C_v} = \frac{C_v + R}{C_v} = \frac{R}{C_v} + 1 \quad \left(\frac{C_p}{C_v} = \gamma \right)$$

$$\gamma - 1 = \frac{R}{C_v}$$

$$\boxed{\gamma = 1 + \frac{R}{C_v}}$$

$$\boxed{\frac{C_p}{C_v} = \gamma}$$

$$(i) C_p > C_v \quad \gamma > 1$$

(ii) C_p, C_v different for different gases.

$$\text{air} \rightarrow C_p = 1 \text{ kJ/kg.K} \quad C_v = 0.72 \text{ kJ/kg.K}$$

$$\gamma_{\text{air}} = \frac{1}{0.72} = 1.4$$

$$\boxed{\gamma_{\text{air}} = 1.4}$$

Enthalpy of gas (H)

$$\boxed{H = U + P.V}$$

Enthalpy properties of gas.

$$dU = U_2 - U_1 \quad , \quad W_{1-2} = PdV = P(V_2 - V_1)$$

$$Q_{1-2} = dU + W_{1-2} = U_2 - U_1 + P(V_2 - V_1)$$

$$Q_{1-2} = (U_2 + PV_2) - (U_1 + PV_1)$$

$$Q_{1-2} = H_2 - H_1$$

Types of Non-flow processes

① Reversible non-flow process

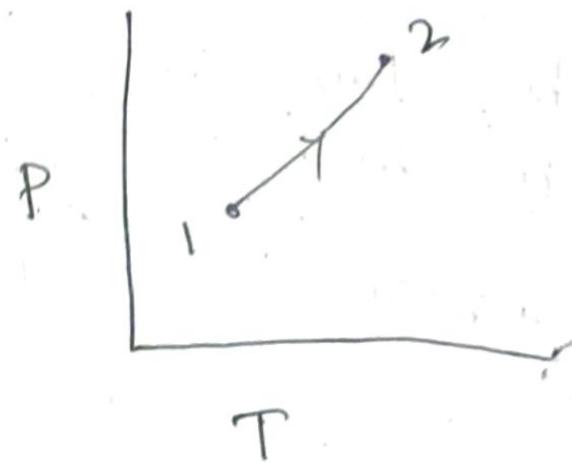
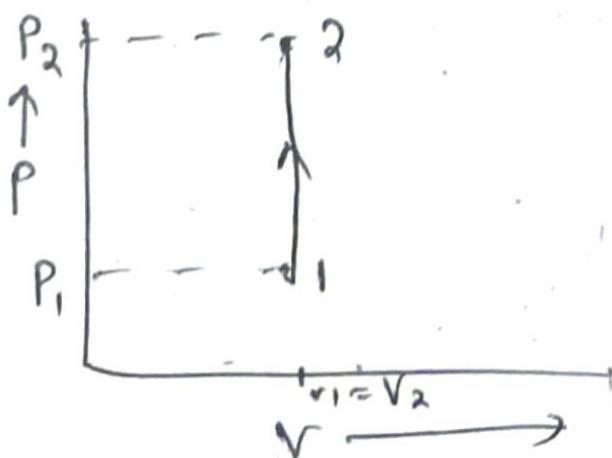
- const. volume process (isochoric)
- const. P (isobaric)
- const. T (isothermal)
- adiabatic
- ~~polytropic~~ process

② Irreversible non-flow process

const. volume process (isochoric)

volume of gas remain constant.

Heat supply \rightarrow increase P & T.



P_1, V_1, T_1 = at state 1
 P_2, V_2, T_2 = " " " 2.

$$V_1 = V_2$$

according to charles Law

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

work done by gas $\delta w = P dV$.

$$\int \delta w = \int P dV = P \int_{V_1}^{V_2} dV$$

$$w_{1-2} = P(V_2 - V_1) = 0 \quad \text{as } (V_1 = V_2)$$

$$w = 0$$

2) change in internal energy.

$$dU = mc_v dT$$

$$\int dU = \int mc_v dT = mc_v \int_{T_1}^{T_2} dT$$

$$U_2 - U_1 = mc_v(T_2 - T_1)$$

③ Heat transfer

$$dQ = dU + dw$$

$$Q_{1-2} = U_2 - U_1 + 0 = mc_v(T_2 - T_1)$$

③ change in enthalpy. $(P_1 V_1 = mRT_1)$

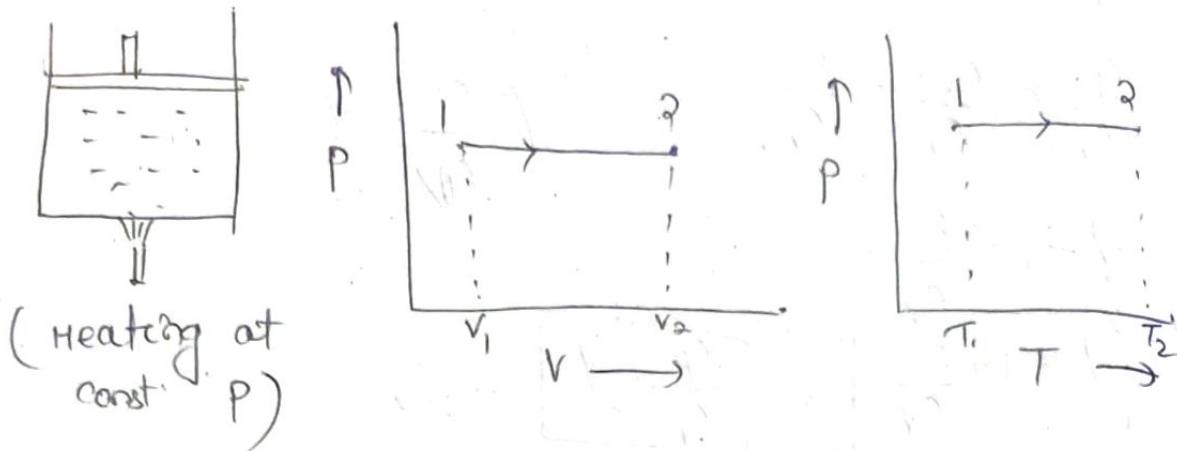
$$dH = dU + d(PV)$$

$$H_2 - H_1 = mc_v(T_2 - T_1) + (mRT_2 - mRT_1) \quad (C_p - C_v = R)$$

$$= mc_v(T_2 - T_1) + mR(T_2 - T_1)$$

$$= m(C_p - C_v)(T_2 - T_1)$$

(b) Const. Pressure process (isobaric process)



Let m kg of gas heated at const. P , from state 1 to state 2.

$$P_1, V_1, T_1 = \text{state 1}$$

$$P_2, V_2, T_2 = \text{state 2}$$

charles's law gas Law

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \quad \frac{V_1}{T_1} = \frac{V_2}{T_2} \quad (\text{charles Law})$$

(1) Workdone by the gas.

$$\delta W = P \delta V$$

$$\int_1^2 \delta W = \int_1^2 P dV = P \int_1^2 dV = P (V_2 - V_1)$$

$$W_{1-2} = P(V_2 - V_1)$$

$$W = mR(T_2 - T_1)$$

$$PV = mRT$$

(2) change in internal energy

$$\int_1^2 dU = \int_1^2 mc_v dT = m c_v (T_2 - T_1)$$

3) Heat transfer or heat supplied.

$$dQ = dU + dw$$

$$\int_1^2 dQ = \int_1^2 dU + \int_1^2 dw$$

$$Q_{1-2} = (U_2 - U_1) + w_{1-2}$$

$$Q_{1-2} = (U_2 - U_1) + P(V_2 - V_1)$$

$$Q_{1-2} = mC_V(T_2 - T_1) + mR(T_2 - T_1)$$

$$Q_{1-2} = m(T_2 - T_1)(C_V + R)$$

$$Q_{1-2} = mC_P(T_2 - T_1) \quad (C_P - C_V = R)$$

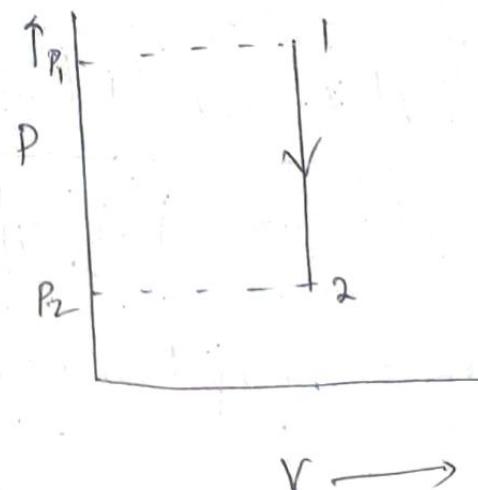
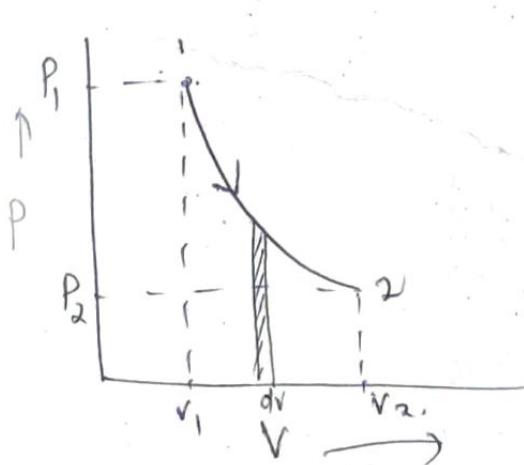
4) Change in enthalpy

$$\int_1^2 dH = \int_1^2 dU + \int_1^2 P d(V)$$

$$H_2 - H_1 = (U_2 - U_1) + P(V_2 - V_1)$$

$$H_2 - H_1 = mC_P(T_2 - T_1)$$

③ Const. temp process (isothermal process)



$$P_1 V_1 T_1 \longrightarrow P_2 V_2 T_2$$

④ Gas eq'

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\therefore P_1 V_1 = P_2 V_2 \longrightarrow \text{Boyle's Law.}$$

(i) workdone by the gas.

$$\delta w = P dV.$$

$$PV = \text{const}$$

$$P_1 V_1 = P_2 V_2 \quad P = \frac{P_1 V_1}{V}$$

$$\delta w = \frac{P_1 V_1}{V} \cdot dV = P_1 V_1 \left(\frac{dV}{V} \right)$$

workdone from state 1 to 2.

$$\int_1^2 dW = \int_1^2 P_1 V_1 \left(\frac{dV}{V} \right)$$

$$\therefore W_{1-2} = P_1 V_1 \int_1^2 \frac{1}{V} dV$$

$$W_{1-2} = P_1 V_1 \left[\ln(V) \right]_1^2$$

$$W = P_1 V_1 \left[\ln(V_2) - \ln(V_1) \right]$$

$$W = P_1 V_1 \ln\left(\frac{V_2}{V_1}\right)$$

$$W = 2.3 P_1 V_1 \log\left(\frac{V_2}{V_1}\right)$$

$\frac{V_2}{V_1}$ = expansion ratio.

$\frac{V_1}{V_2}$ = compression ratio.

$$P_1 V_1 T_1 \longrightarrow P_2 V_2 T_2$$

④ Gas eq'

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\therefore P_1 V_1 = P_2 V_2 \longrightarrow \text{Boyle's Law.}$$

(i) workdone by the gas.

$$\delta w = P dV.$$

$$PV = \text{const}$$

$$P_1 V_1 = P_2 V_2 \quad P = \frac{P_1 V_1}{V}$$

$$\delta w = \frac{P_1 V_1}{V} \cdot dV = P_1 V_1 \left(\frac{dV}{V} \right)$$

workdone from state 1 to 2.

$$\int_1^2 dW = \int_1^2 P_1 V_1 \left(\frac{dV}{V} \right)$$

$$\therefore W_{1-2} = P_1 V_1 \int_1^2 \frac{1}{V} dV$$

$$W_{1-2} = P_1 V_1 \left[\ln(V) \right]_1^2$$

$$W = P_1 V_1 \left[\ln(V_2) - \ln(V_1) \right]$$

$$W = P_1 V_1 \ln\left(\frac{V_2}{V_1}\right)$$

$$W = 2.3 P_1 V_1 \log\left(\frac{V_2}{V_1}\right)$$

$\frac{V_2}{V_1}$ = expansion ratio.

$\frac{V_1}{V_2}$ = compression ratio.

2) Change in internal energy :-

$$dU = mc_v dT$$

from 1 to 2.

$$\int_1^2 dU = \int_1^2 mc_v dT = mc_v (T_2 - T_1)$$

as $T_1 = T_2$

$$U_2 - U_1 = 0$$

$$U_1 = U_2$$

3) Heat transferred or heat supplied

$$dQ = dU + dw$$

$$\int_1^2 dQ = \int_1^2 dU + \int_1^2 dw$$

$$Q_{1-2} = (U_2 - U_1) + w_{1-2}$$

$$Q_{1-2} = w_{1-2}$$

\Rightarrow adiabatic process

$$(1) \text{ work done} = \frac{P_1 V_1 - P_2 V_2}{n-1}$$

2) Internal energy

$$dU = mc_v dT$$

3) Heat transfer $Q = 0$

4) Enthalpy $= mc_p dT$

Polytropic process

$$(1) w = \frac{P_1 V_1 - P_2 V_2}{n-1}$$

$$(2) dU = mc_v dT$$

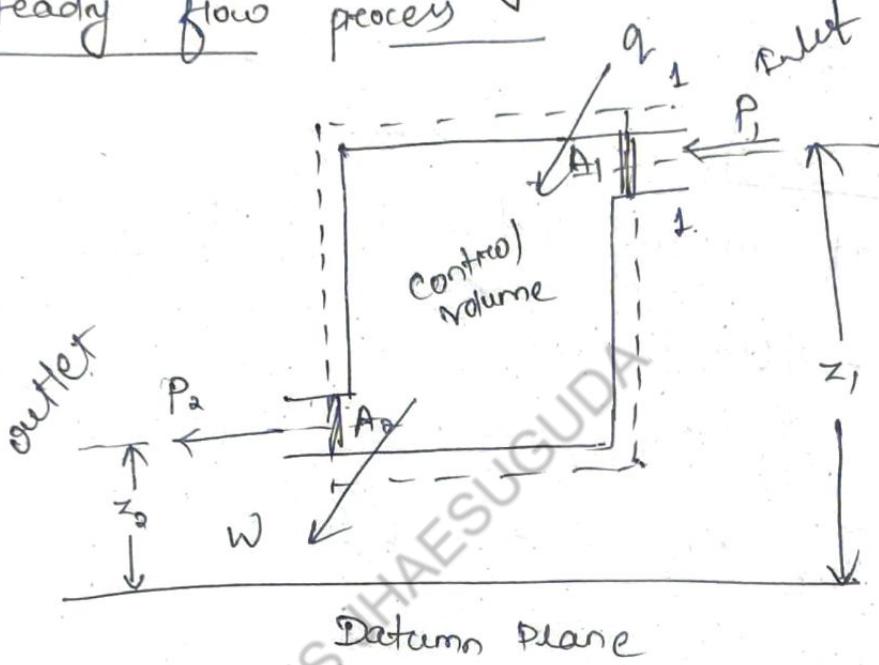
$$(3) Q = \frac{n-1}{n-1} \left(\frac{P_1 V_1 - P_2 V_2}{n-1} \right)$$

$$(4) dH = mc_p (T_2 - T_1)$$

1st Law of Thermodynamic applied to flow process.

- (1) steady flow process $\rightarrow m_i = m_o, E = \text{const}$
- (2) unsteady flow " $\rightarrow m_i \neq m_o, E = \text{change}$

2nd Law of thermodynamics applied to steady flow process



Working substance enter at 1-1
with velocity v_1 , pressure P_1 ,

specific volume $= v_{s1}$

specific internal energy $= u_1$

① Heat transfer q_{1-2}

② Work transfer w_{1-2}

③ $\Delta P.E = \rho g z$

energy accompanying unit mass flow

$$(1) P.E = \rho g z \quad (\text{N-m/kg or J/kg})$$

$$(2) K.E = \frac{v^2}{2}$$

- (3) ~~remaining~~ internal energy i.e. u . (J/kg)
 4) flow energy Pv_s ($N\cdot m/kg$)

$$e_1 = gz_1 + \frac{v_1^2}{2} + u_1 + p_1 v_{s1} + q_{1-2} \quad (J/kg)$$

$$e_2 = gz_2 + \frac{v_2^2}{2} + u_2 + p_2 v_{s2} + w_{1-2} \quad (J/kg)$$

$$e_1 = e_2$$

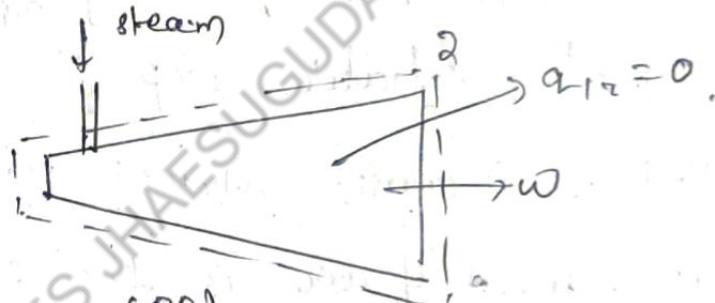
$$h_1 = u_1 + p_1 v_{s1}$$

$$h_2 = u_2 + p_2 v_{s2}$$

$$gz_1 + \frac{v_1^2}{2} + h_1 + q_{1-2} = h_2 + w_{1-2}$$

S.F.E.E

turbine



~~SPDP~~

$$z_1 = z_2 \quad (\text{PE})$$

$$v_1 = v_2 \quad (\text{KE})$$

$$q_{1-2} = 0$$

$$\therefore w_{1-2} = h_1 - h_2$$

Compress

$$\therefore w_{1-2} = (h_1 - h_2) - q_{1-2}$$

~~No~~ q_{1-2} is negative.

Q) A closed vessel contains 2 kg of CO_2 at a temp. of 20°C & a pressure of 0.7 bar. Heat is supplied to the vessel till the gas acquires a pressure of 1.4 bar calculate the value of heat supplied. $c_v = 0.657 \text{ kJ/kgK}$.

$$\rightarrow m = 2 \text{ kg}$$

$$T = 20^\circ\text{C} + 273 = 293 \text{ K}$$

$$P_1 = 0.7 \text{ bar}$$

$$P_2 = 1.4 \text{ bar}$$

$$c_v = 0.657 \text{ kJ/kgK}$$

$$\frac{P_1}{T_1} = \frac{P_2}{T_2} \quad \therefore T_2 = \frac{P_2 \times T_1}{P_1} = \frac{1.4 \times 293}{0.7} = 586 \text{ K}$$

$$Q_{12} = m c_v (T_2 - T_1)$$

$$= 2 \times 0.657 (586 - 293)$$

$$= 385 \text{ kJ}$$

(g) One kg of air is expanded at a constant pressure of 2.5 bar from a volume of 0.3 m^3 to a volume of 0.45 m^3 .

Find (1) External workdone by gas

(2) Internal Energy of gas

(3) Heat transfer during process.

$$\rightarrow m = 1 \text{ kg}$$

$$P = 2.5 \text{ bar} = 250 \times 10^3 \text{ N/m}^2 \quad R = 287 \text{ J/kg K}$$

$$V_1 = 0.3 \text{ m}^3$$

$$V_2 = 0.45 \text{ m}^3$$

Specific heat at constant volume $C_V = 0.72 \text{ kJ/kg}$

$$C_p = 1.005 \text{ kJ/kg}\cdot\text{K}$$

$$P_1 V_1 = m R T_1$$

$$T_1 = \frac{P_1 V_1}{m R} = \frac{250 \times 10^3 \times 0.3}{1 \times 287} = 261 \text{ K}$$

~~$$T_2 = \frac{P_2 V_2}{m R} = \frac{250 \times 10^3 \times 0.45}{1 \times 287} = 392 \text{ K}$$~~

(I) External work done by gas $w = P(V_2 - V_1)$

$$w = 250 \times 10^3 (0.45 - 0.3) = 37.5 \text{ kJ}$$

(II) Internal Energy of the gas

$$\Delta U = m C_V (T_2 - T_1) = 1 \times 0.72 (392 - 261) = 94.32 \text{ kJ}$$

(III) Heat transferred

$$Q_{12} = m C_p (T_2 - T_1) = 1 \times 1.005 (392 - 261) = 131.6 \text{ kJ}$$

Q) If a Hg barometer reads 720 mm Hg. find atm pressure in kPa.

→ Barometric reading = 720 mm Hg

$$1 \text{ mm of Hg} = 133.3 \text{ N/m}^2$$

$$\begin{aligned} \text{atm pressure} &= 720 \times 133.3 = 95976 \text{ N/m}^2 \\ &= \frac{95976}{1000} = 95.976 \text{ kPa} \end{aligned}$$

Q) Steam leaving turbine at a pressure = 70 kPa vacuum and absolute pressure in bar if atm pressure is 101 kPa.

→ vacuum pressure = 70 kPa

$$\text{atm pressure} = 101 \text{ kPa}$$

$$\text{Abs p} = \text{atm p} - \text{vacuum p}$$

$$\approx 101 - 70 = 31 \text{ kPa} \quad (1 \text{ bar} = 100 \text{ kPa})$$

$$= \frac{31}{100} \text{ bar} = 0.31 \text{ bar}$$

Free Expansion process :-

- Most of thermodynamic processes become irreversible due to presence of friction, turbulence etc. The effect of irreversibility is loss of work, i.e. in compression process more work is to be supplied than the reversible work, whereas in expansion process, less work is obtained from the system.
- free-expansion occurs when a fluid is allowed to expand suddenly into a vacuum chamber through an orifice

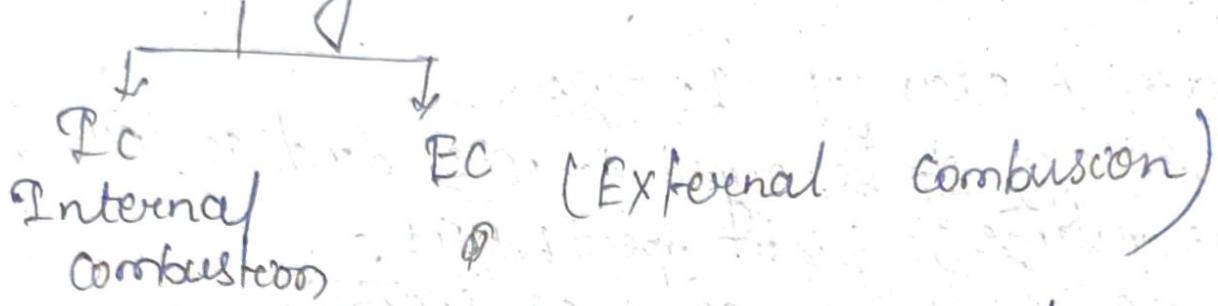
- of large size.
- In this process, no heat is supplied or rejected & no external work is done.
 - Enthalpy of the fluid constant.
 - This type of expansion called a Constant enthalpy process or free expansion process.

$$Q_{12} = 0, W_{12} = 0, du = 0$$

I.C. ENGINE

chapter-4

Heat Engine

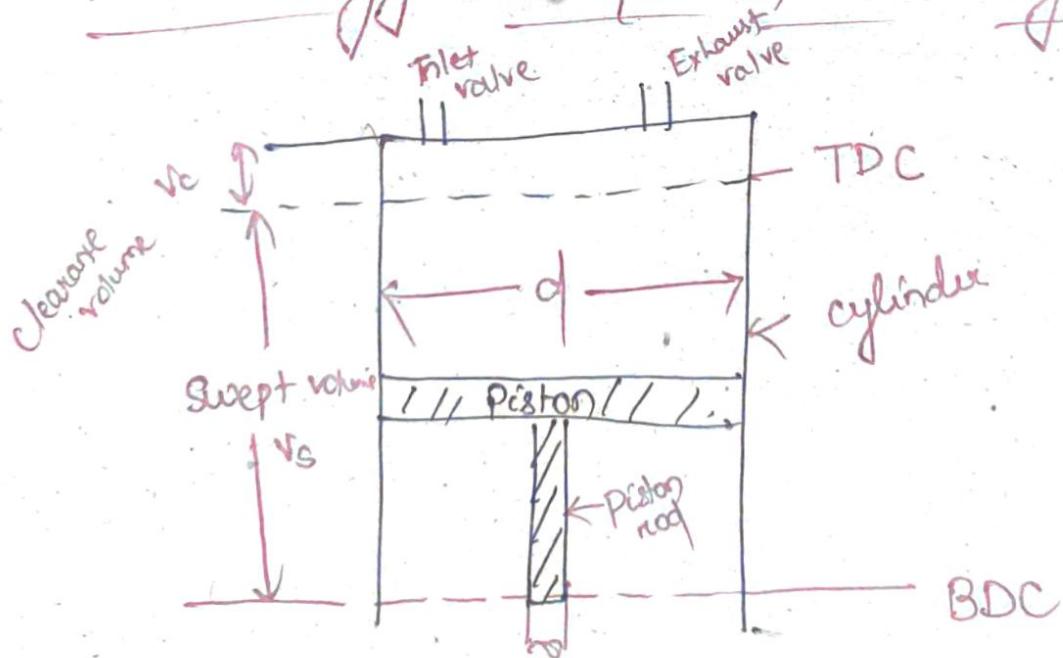


Heat Engine :- Heat Engine is a thermodynamic system used for converting heat into work, while operating in a cycle betⁿ source & sink.

I.C. Engine :- It is a heat engine in which combustion of fuel occurs inside the engine cylinder.

External combustion Engine :- It is a heat engine where a working combustion take place outside the engine cylinder.

Terminology used in I.C. engine:



Bore: diameter of cylinder or piston
stroke: distance move by piston in one direction.
 $TDC \rightarrow BDC$ or $BDC \rightarrow TDC$.

$$\text{STROKE} = 2 \times \text{radius of crank}$$

TDC = it is extreme position of piston near to head.

BDC = it is extreme position of piston opposite to head.

clearance volume = it is the minimum volume of clearance bet' cylinder head & the piston at TDC position.

Swept volume or stroke volume (V_s)

It is the max volume swept by the piston in moving from TDC to BDC & vice-versa.

$$\text{Swept volume} = V_s = \frac{\pi}{4} d^2 \times l$$

Total volume or full cylinder volume = (V)

Total volume is sum of clearance volume (V_c) plus swept volume (V_s).

$$V = V_c + V_s$$

clearance ratio (c)

$$C = \frac{V_c}{V_s} = \frac{\text{clearance volume}}{\text{swept volume}}$$

compression or expansion ratio

$\text{r} = \frac{\text{total volume } (V)}{\text{Clearance Volume } (V_c)}$

Clearance Volume (V_c)

$$r = \frac{V_c + V_s}{V_c} = 1 + \frac{V_s}{V_c} = 1 + \frac{1}{c}$$

b) mean effective pressure (P_m)

Let c_3 be the avg. pressure acting on the piston during working stroke.

$$P_m = \frac{\text{workdone}}{\text{swept volume}} = \frac{W}{V_s}$$

$$P_m = \frac{W}{\frac{\pi}{4} d^2 \times l} = \frac{4W}{\pi d^2 l}$$

i) Arc standard efficiency :-

$$\eta = \frac{\text{workdone}}{\text{Heat supplied}} = \frac{\text{Heat supplied} - \text{Heat reject}}{\text{Heat supplied}}$$

ii) Relative efficiency :-

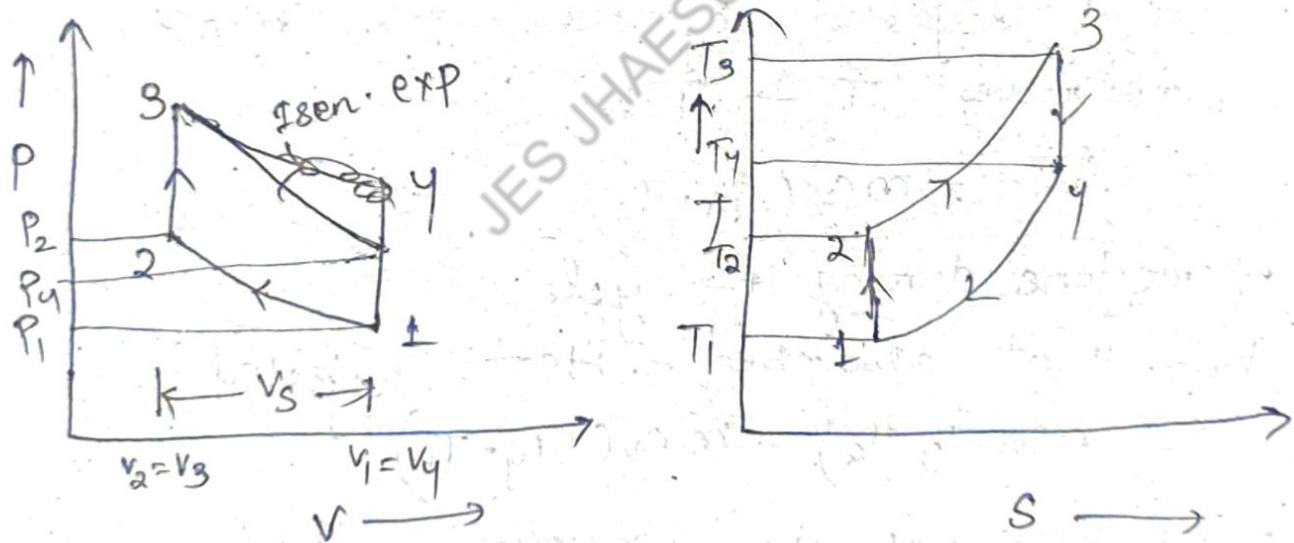
$$\eta_R = \frac{\text{Actual thermal efficiency}}{\text{Arc standard efficiency.}}$$

OTTO cycle (constant volume cycle)

- This cycle is used for spark ignition (SI) internal combustion engines.
- Heat received & rejected at const. volume. Therefore, this cycle is known as const. volume cycle.
- OTTO cycle consists of two const volume & two reversible adiabatic process.

m = mass of air in the engine cylinder at point 1, when piston at BDC.

$P_1, V_1, T_1 = P, V, T$ of air at 1.



Process - 1-2

- Reversible adiabatic compression process.
- piston moves from BDC \rightarrow TDC.
- air compressed in reversible adiabatic manner.
- T rises from $T_1 \rightarrow T_2$.
- No heat rejected or absorbed by air

Process - 2-3

→ piston is rest at TDC.

→ Heat absorbed by air & Temp of air increases $T_2 \rightarrow T_3$.

$$\text{Heat absorbed } Q_{23} = m_c v (T_3 - T_2)$$

Process - 3-4 reversible adiabatic expansion process

$$\rightarrow TDC \rightarrow BDC$$

→ Temp decrease $T_3 \rightarrow T_4$

→ No heat is absorbed or rejected

process - 4-1 → const volume cooling process

→ heat rejected by the air & temp decreases $T_4 \rightarrow T_1$

$$Q_{41} = m_c v (T_4 - T_1)$$

Work done during the cycle,

$W = \text{Heat absorbed} - \text{Heat rejected}$

$$= m_c v (T_3 - T_2) - m_c v (T_4 - T_1)$$

ideal efficiency $\eta = \frac{\text{Workdone}}{\text{Heat absorbed}}$

$$\eta = \frac{m_c v (T_3 - T_2)}{m_c v (T_3 - T_2) - m_c v (T_4 - T_1)}$$

$$= 1 - \frac{T_4 - T_1}{T_3 - T_2}$$

The ratio of compression & expansion are equal.

$$\frac{V_1}{V_2} = \frac{V_4}{V_3} = r$$

reversible adiabatic compression process 1-2

$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{\gamma-1} = \left(\frac{1}{r}\right)^{\gamma-1}$$

For reversible adiabatic expansion process 3-4

$$\frac{T_4}{T_3} = \left(\frac{V_3}{V_4}\right)^{\gamma-1} = \left(\frac{1}{r}\right)^{\gamma-1}$$

$$\frac{T_4}{T_2} = \frac{T_4}{T_3} \text{ or } T_4 = \frac{T_1 T_3}{T_2}$$

$$\eta = 1 - \frac{T_1 T_3 - T_1}{T_2} = 1 - \frac{T_1 T_3 - T_1 T_2}{T_2 (T_3 - T_2)}$$

$$\eta = 1 - \frac{T_1}{T_2} = 1 - \left(\frac{1}{r}\right)^{\gamma-1}$$

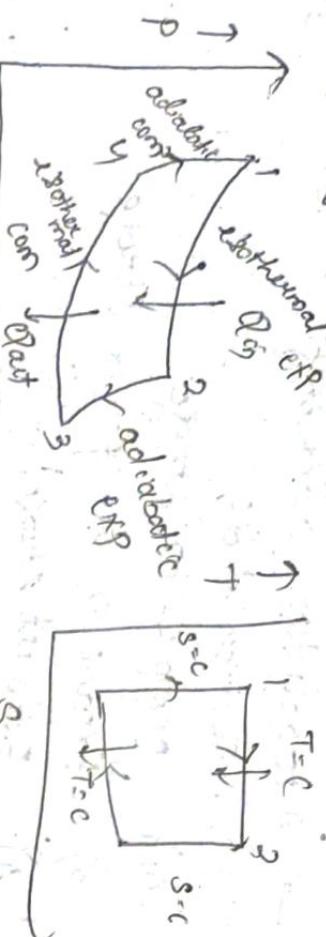
Carnot cycle

→ theoretical ideal thermodynamic cycle it provide upper limit on the efficiency that thermodynamic engn can achieve during conversion of heat to work.

$$\rightarrow \eta_{\text{Carn}} < \eta_{\text{rev}}$$

→ All reversible Heat Engine are same working betw same two temp.

Cannot cycle



$$\eta = \frac{\text{Workdone}}{\text{Heat supplied}} = \frac{Q_S - Q_R}{Q_S}$$

1-2 Reversible Isothermal expansion of the gas

$$\text{at 'hot' temp } w = P_1 V_1 \ln \left(\frac{V_2}{V_1} \right) \quad (T_2 : C)$$

2-3 Isoentropic expansion of gas

$$(isolation) (S=C) = -n_C \left(\frac{V_2}{T_2} - \frac{V_1}{T_1} \right)$$

3-4 Reversible Isothermal compression at 'cold' temp T_1

$$- w = n_C R \left(T_2 - T_1 \right)$$

$$w = P_2 V_2 \ln \left(\frac{V_1}{V_2} \right)$$

$$w = n_C R T_2 \ln \left(\frac{V_2}{V_1} \right) - n_C v \left(T_2 - T_1 \right) + n_C R T_1 \ln \left(\frac{V_1}{V_2} \right)$$

$$= n_C R T_2 \ln \left(\frac{V_2}{V_1} \right) - n_C R T_1 \ln \left(\frac{V_2}{V_1} \right)$$

$$= n_C R T_2 \ln \left(\frac{V_2}{V_1} \right) - n_C R T_1 \ln \left(\frac{V_2}{V_1} \right)$$

for adiabatic expansion of ideal gas (2-3)

$$C_v \ln \left(\frac{T_2}{T_1} \right) = R \ln \left(\frac{V_3}{V_2} \right)$$

$$C_v \ln \left(\frac{T_2}{T_1} \right) = R \ln \left(\frac{V_4}{V_3} \right)$$

Heat supplied ($T=c$) $Q_{12} = P_1 V_1 \ln\left(\frac{V_2}{V_1}\right)$
 $\underline{(1-2)}$ $= mRT_1 \ln\left(\frac{V_2}{V_1}\right)$

$\frac{V_2}{V_1} = r_c = \text{compression ratio}$ $Q_{12} = mRT_1 \ln(r) \quad \textcircled{1}$

Heat Rejection ($T=c$) $Q_{34} = P_3 V_3 \ln\left(\frac{V_4}{V_3}\right)$
 $\underline{(3-4)}$ $= mRT_3 \ln\left(\frac{V_3}{V_4}\right)$

$\frac{V_3}{V_4} = \text{compression ratio}$ $\underline{\underline{= mRT_3 \ln(r)}} \quad \textcircled{2}$

Net work = $HS - HR$
 $= mRT_1 \ln(r) - mRT_3 \ln(r)$
 $= mR \cancel{\ln(r)} (T_1 - T_3) \quad \textcircled{3}$

$\eta = \frac{NW}{HS} = \frac{mR \ln(r) (T_1 - T_3)}{mRT_1 \ln(r)}$

$\eta = \frac{T_1 - T_3}{T_1}$

$T_3 = \text{Lower temp}$

$\boxed{\begin{array}{l} \text{cannot} \\ \text{cycle} \end{array}} = 1 - \frac{T_3}{T_1} = 1 - \frac{T_{\text{lower}}}{T_{\text{higher}}} \quad \begin{array}{l} T_1 = \text{Higher temp.} \\ \text{---} \end{array}$

η of Otto cycle depends on compression ratio π .

$$\eta \uparrow \quad \pi \uparrow$$

3) Diesel cycle (const. pressure cycle)

→ Dr Rudolph Diesel

→ 1893

→ CI → diesel fuel

→ Heat is supplied at const. P' . So it's called const. pressure cycle.

→ ① → ② → ③ → ④ → ①

const. volume.

$$Q_{23} = 0$$

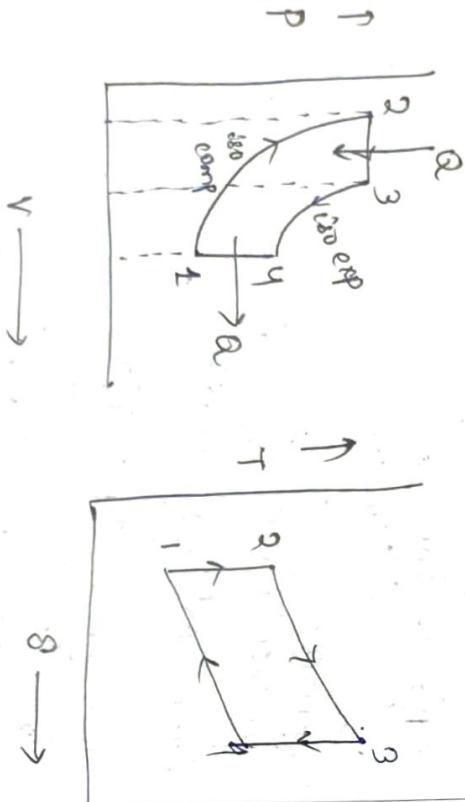
$$\frac{T_2}{T_3} = \left(\frac{P_2}{P_3}\right)^{\frac{1}{\gamma-1}}$$

④ (4-1) const. volume heat rejection :- $4 \rightarrow 1$.

$$T_4 \rightarrow T_1 (\downarrow)$$

Heat rejected by air

$$Q_{41} = m_c (T_4 - T_1)$$



$v \longrightarrow$

$s \longrightarrow$

m = mass of air (kg) in engine cylinder.

P, v, T

$$\text{BDC} \rightarrow \text{TDC}$$

$$\frac{T_1}{T_2} \rightarrow T_2 (1) \quad Q = 0$$

$$\left(\frac{T_1}{T_2}\right) = \left(\frac{v_2}{v_1}\right)^{\frac{1}{\gamma-1}} = \left(\frac{1}{\pi}\right)^{\frac{1}{\gamma-1}}$$

$$T_2 = T_1 \cdot \pi^{\frac{1}{\gamma-1}}$$

$$\text{Process } 2-3 \quad (\text{const. pressure heat addition})$$

piston moves from 2 to 3. More heat is added at '3' supply of heat is cutoff so '3' point is called cutoff point.

$Q_{23} = m_c P (T_3 - T_2)$
 C_p = specific heat of air at const. pressure.

⑤ process 3-4 (rev. adiabatic expansion)
 cutoff point \rightarrow BDC

$$T_3 \rightarrow T_4 (\downarrow)$$

$$Q_{34} = 0$$

W = Heat absorbed - heat rejected.

$$= mcp(T_3 - T_a) - mc_v(T_4 - T_i)$$

$$\eta = \frac{\text{Workdone}}{\text{Heat supplied}}$$

$$= \frac{mcp(T_3 - T_a) - mc_v(T_4 - T_i)}{mc_p(T_2 - T_a)}$$

$$\eta = 1 - \frac{c_p}{cp} \left(\frac{T_4 - T_i}{T_3 - T_a} \right) \quad \text{--- (1)}$$

$$\eta = 1 - \frac{g}{r} \left(\frac{T_4 - T_i}{T_3 - T_a} \right) \quad \text{--- (2)}$$

r_c = compression ratio = $\frac{V_1}{V_2}$

g = cut-off ratio = $\frac{V_3}{V_2}$

$$r_i = \text{expansion ratio} = \frac{V_4}{V_3} = \frac{V_i}{V_3} = \frac{V_i}{V_2} \times \frac{V_2}{V_3}$$

$$\frac{1-g}{r} = \frac{r}{g}$$

$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{g-1} = \left(\frac{1}{r}\right)^{g-1}$$

$$T_2 = T_1 r^{g-1} \quad \text{--- (3)}$$

$$\frac{2-3}{\overline{3-4}} \frac{V_2}{T_2} = \frac{V_3}{T_3} = g \cdot T_2 = g \cdot T_1 \cdot r^{g-1} \quad \text{--- (4)}$$

$$T_3 = \frac{V_3}{V_2} T_2 = g \cdot T_2 = g \cdot T_1 \cdot r^{g-1} \quad \text{--- (5)}$$

$$\frac{T_4}{T_3} = \left(\frac{V_4}{V_3}\right)^{g-1} = \left(\frac{1}{r_i}\right)^{g-1} = \left(\frac{g}{r}\right)^{g-1}$$

$$T_4 = T_3 \left(\frac{g}{r}\right)^{g-1} = g \cdot T_3 \cdot r^{g-1} \cdot \left(\frac{g}{r}\right)^{g-1} = g \cdot T_1 \cdot g^g \quad \text{--- (6)}$$

$$\begin{aligned} \eta &= 1 - \frac{1}{2} \left(\frac{T_4 - T_i}{T_3 - T_a} \right) \\ &= 1 - \frac{1}{2} \left(\frac{T_1 g^g - T_i}{g T_1 \cdot r^{g-1} - T_1 \cdot r^{g-1}} \right) \end{aligned}$$

$$\eta = 1 - \frac{T_1 (g^g - 1)}{2 T_1 r^{g-1} (g-1)}$$

$$\boxed{\eta = 1 - \frac{T_1 (g^g - 1)}{2 T_1 r^{g-1} (g-1)}}$$

* * * \rightarrow ~~so~~ $\eta \propto 1/g$, so $\eta \uparrow g \uparrow$.

* * * η (compression ratio) = $\eta_{\text{Otto cycle}} / \eta_{\text{diesel cycle}}$

$\rightarrow g = f$, ~~so~~ $f \propto 1/g$, so $f \downarrow g \downarrow$.
 compression ratio for diesel cycle $14 < r_c < 18$.

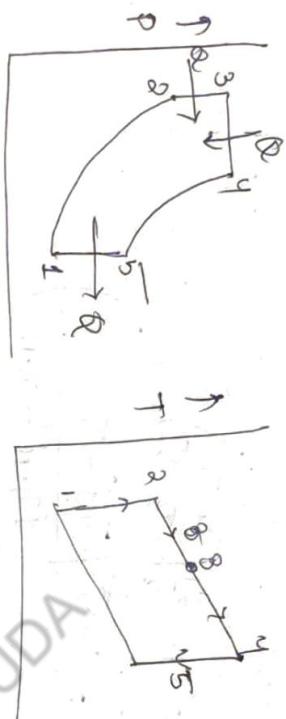
Dual cycle

→ Combination of Otto cycle & Diesel cycle.

→ ② rev. adiabatic process

& const. volume process.

1 const. pressure process.



\rightarrow

$S \rightarrow$

1-2 (rev. adiabatic compression process)

TDC \rightarrow TDC

$T_1 \rightarrow T_2 (\uparrow)$

$Q_{1,2} = 0$

2-3 const. volume heat addition,

$T_2 \rightarrow T_3 (\uparrow)$

$Q_{2,3} = m_C V(T_3 - T_2)$

3-4 const. pressure heat addition,

$T_3 \rightarrow T_4 (\uparrow)$

$Q_{3,4} = m_C p (T_4 - T_3)$

4-5 rev. adiabatic expansion process

$T_4 \rightarrow T_5 (\downarrow)$ $Q_{4,5} = 0$

Process 5-1 const. volume heat rejection,
 $Q_{5-1} = m_C v (T_5 - T_1)$

\dot{W} = Heat absorbed - heat rejected.

$$\dot{W} = (Q_{2,3} + Q_{3,4}) - Q_{5-1}$$

$$\eta = \frac{\dot{W}}{\text{Q supplied}}$$

$$\eta = 1 - \frac{(dp^{\beta-1})}{r^{1-\beta} [(dp^{-1}) + \beta dp(\beta-1)]}$$

$$\tau = \text{compression ratio} = \frac{V_1}{V_2}$$

$$\frac{dp}{dt} = \text{pressure ratio} = \frac{p_3}{p_2}$$

$$\frac{f}{r} = \frac{V_2}{V_3} = \frac{V_1}{V_2} = \text{cutoff ratio}$$

~~Gasoline~~ > Dual > Diesel (Same compression ratios)

Diesel > Dual > Gasoline (Same max p & T)

Fuel & combustion

(1) Define fuel

- Fuel is simply a combustible substance which burns in the presence of oxygen & release heat energy.
- Various types of fuel are solid, liquid & gas.
- Most of fuel contain carbon & hydrogen as main constituent they are called hydrocarbon fuels. C_nH_m
- Each fuel consists of certain amount of bonded energy → Chemical energy & it is in the form of internal energy.
- In combustion the interatomic bonds of the molecules of the fuel & O_2 are broken & rearrangement of atoms in new molecular combination takes place.
- During this process energy release in the form of heat → total no. of atom remain unchanged → Law of conservation of mass.

Types of fuel

Characteristic of an Ideal fuel

- (i) It should have a high heating value.
- (ii) free from moisture & non-combustible matter.
- (iii) not harmful & pollutant
- (iv) moderate ignition temp.
- (v) easy to transport & store & minimum space.
- (vi) High combustion efficiency
- (vii) Low cost.

Classification of fuel

Solid fuel - Coal

Peat - wood + vegetable matter.

- 30% moisture.

- calorific value - 14,500 KJ/kg

Lignite - volatile matter + moisture + low carbon %

- brown colour

- high ash & low heating value.

- calorific value - 21,000 KJ/kg.

- heavy smoke

Fuel & combustion

→ Fuel is a substance which release heat energy when burn at sufficient high temp.

use of fuel

- (i) use in power plant
- (ii) Industrial purpose.
- (iii) Blast furnace.

Fuel constituent

All fuel contain Hydrogen & carbon.
fuel usually contain

- (i) Hydrogen
- (ii) Carbon
- (iii) Sulphur
- (iv) Oxygen
- (v) Nitrogen
- (vi) Ash

Characteristic of fuel

- (i) Easy ignition.
- (ii) High heating value (calorific value)
- (iii) Low smoke emission.
- (iv) Easily combustible combustion properties.

Types of fuels

(i) According to physical state

a) Solid b) Liquid c) Gas

ii) According to the nature of origin.

Solid fuel

→ fuels which are found in their solid state at room temp.

e.g. wood, charcoal, straw, wood...

Advantages:

→ easier transportation & storage.
→ low production cost.

→ moderate ignition temp.

Disadvantages:

→ large energy is wasted.
→ handling & controlling cost high.
→ Ash content is high.

Liquid fuel

→ most liquid fuels are derived from the remains of dead plants & animals by exposure to heat & pressure in earth's crust.

e.g. petrol, gasoline, kerosene
diesel oil, petrol

Advantages:

i) High calorific value.
ii) burn without ash.

iii) easy transportation.

iv) required less space.

disadvantages:

i) high cost as compare to solid fuel.
ii) storage methods are costlier.
iii) risk of fire.

Gaseous fuel

→ Gaseous fuel are occur in nature.
most gaseous fuels are composed of hydrocarbons, carbon monoxide, hydrogen mixture of them all.

e.g. - Natural gas, coal gas, coke oven gas.

Advantage:

i) Transportation through pipe is easy.

ii) high heat content.
iii) clean after use.

Disadvantages:

i) Large storage tank required.
ii) high & strict safety measures
need to followed.

Heating value of fuel

→ Heating value / calorific value of a fuel is defined as the total quantity of heat liberated by the complete combustion of unit quantity of fuel.

$$\rightarrow \text{for solid or liquid} = \frac{\text{KJ}}{\text{kg}}$$

$$\rightarrow \text{For gaseous fuel} = \frac{\text{KJ}}{\text{m}^3}$$

$$\rightarrow \text{CV may be expressed by two values}$$

a) Higher calorific value (HCV)

b) Lower calorific value (LCV)

Higher calorific value

→ it is defined as the total amount of heat liberated when unit quantity of fuel is completely burnt the product of combustion are cooled to room temperature.

Lower calorific value :-

→ it is defined as the amount of heat liberated by complete combustion of unit quantity of fuel &

The products of combustion are not cooled at room temp but allowed to escape in atmosphere.

$$\text{LCV} = \text{HCV} - m_s L \quad \text{KJ/kg}$$

m_s = mass of water vapour formed per kg of fuel burnt

$$L = \frac{\text{Latent heat of water}}{\text{Latent heat of water vapour}} \quad \text{at } 15^\circ\text{C.}$$

$$\rightarrow \text{ECP} -$$

$$\text{HCV} = \text{LCV} + \left(\frac{9 \times h \times \text{Latent heat of water}}{100} \right)$$

$$h = \% \text{ of hydrogen in fuel.}$$

To define the Quality of fuel.

Octane no.

→ octane no. indicates the tendency of octane (petrol) fuels to knock. Higher is the octane no., the more difficult the auto-ignition.

→ Standard fuel combination

- a) iso-octane
- b) n-heptane

→ if during compression

petrol engine

stroke fuel is more than that of its auto-ignition temp. it will burn before heat supply due to spark plug.

→ Due to this knocking tendency takes place in engine.

→ so fuel quality should be such that during compression stroke it will not reach its auto ignition temp.

(self ignition)

→ The quality of petrol which reduce its knocking auto ignition tendency & knocking properties is known as octane no.

more ↑ octane no. ↑ good quality of fuel.

→ iso-octane) n-heptane

(↑anknock) (↓anknock)

→ 1% of iso-octane → its octane no.
→ octane no. 90 mean → 90% iso-octane
→ 10% n-heptane

Cetane no.

→ Quality of diesel fuel.

→ 55% cetane + methyl-naphthalene 45% - cetane in fuel called

cetane no.

→ after fuel spray to before fuel combustion called ignition delay.

→ the cetane no. of diesel means its ignition delay should be less so that fuel burn early.

- Octane no.
- Petrol performance / quality of petrol.
 -
 -
 - ① damage piston, cylinder, connecting rod
 - India = $\frac{\text{speed}}{\text{speed} + \text{speed}}$ 93
 - during compression stroke charge temp is high (reached autoignition temp)
 - if ~~extra~~ fuel burns before using spark plug.
 - to reduce knocking in engine, we must consider ~~lower~~ see there should not be autoignition temp, in the fuel.
 - ~~on~~ petrol antiknock properties is called octane no.

- Cetane no.
- Performance of diesel fuel
- India 47 - 51
 - n-hexadecan ($C_{16}H_{34}$) → cetane
 - methyl napthalene
 - ~~55~~ 55% cetane if has 55% cetane & rest methyl napthalene.
 - ignition delay (\downarrow)

- octane no. ↑ antiknock ↑
- best petrol
- ① iso-octane (anti knock properties)
 C_8H_{18} (% of this shows octane, of fuel)
- ② n-heptane (\downarrow)

set 93 + isoctane no.

93% — isoctane
 $\pm \%$ — n-heptane

e.g. = 105 %
100% isoctane
5% more pure octane isoctane.